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The ENSO Cycle and Forecastability of Global Inflation and Output Growth: Evidence from Standard and Mixed-Frequency Multivariate Singular Spectrum Analyses

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The ENSO Cycle and Forecastability of Global Inflation and Output Growth: Evidence from Standard and Mixed-Frequency Multivariate Singular Spectrum Analyses

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ABSTRACT

In this paper the role of the El Niño-Southern Oscillation (ENSO), measured by the Equatorial Southern Oscillation Index (EQSOI), is used to formally forecast the inflation and GDP growth rates of the United States (US), advanced (excluding the US) and emerging countries, as well as the world economy (barring the US). We rely on univariate and multivariate Singular Spectrum Analyses (SSA), as well as mixed-frequency version of the latter since the EQSOI is monthly, while GDP is available only at quarterly frequency unlike monthly inflation rates. We find statistically significant evidence of the ability of the EQSOI in forecasting inflation and GDP growth rates of the four economic blocs, though there are exceptions in terms of forecasting gains associated with inflation rate of emerging economies and the growth rate of the US. Our results have important implications for policymakers.

KEYWORDS

GDP growth; Inflation; ENSO; Forecastibility; Mixed-Frequency Multivariate SSA; Continuous Wavelet Transform. *JEL*: C22; C32; E31, E32; E37; Q54.

1 1. Introduction

The El Niño-Southern Oscillation (ENSO) is an irregularly periodic variation in winds 2 and sea surface temperatures over the tropical eastern Pacific Ocean, which tends to 3 affect the climate of much of the tropics and subtropics 30. The warming phase 4 of sea temperature is known as El Niño and the cooling phase as La Niña. Each of 5 these two phases can last several months and typically occur every few years with 6 varying intensities per phase. However, it would be a mistake to think of the ENSO 7 as merely affecting climate patterns, but instead, some studies have highlighted its 8 ability to produce downturn phases of the business cycle to some degree, but primarily 9 causing inflationary impacts via increases in agricultural commodity and crude oil 10 prices 11, 22, 53, 66, 99, 233, 255, 288, due to El Niño and La Niña events producing major 11 global rare disaster risks historically 7, 14, 26. 12

¹³ While these studies are of tremendous importance in deducing the empirical link

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between ENSO and major macroeconomic variables, i.e., growth and inflation, these 14 primarily being in-sample (causal and structural) analyses are to some degree of limited 15 value to policymakers in general, and central banks in particular, who would need 16 accurate predictions of the future path of key economic variables, i.e., out-of-sample 17 forecasts, while making their policy decisions, following episodes of weather-related 18 uncertainties. Moreover, from a statistical perspective, it is well-established that in-19 sample predictability does not guarantee out-of-sample forecasting gains emanating 20 from a specific predictor, besides the fact that it is out-of-sample forecasting that 21 tends to provide a more robust test of the appropriateness of an econometric model 22 and the predictor 3. Given this, the objective of this paper is to provide for the first 23 time an out-of-sample forecasting analysis of output growth and inflation based on the 24 information content of the ENSO cycle for not only the United States (US), but also 25 regional blocs involving other advanced (excluding the US) and emerging economies, 26 besides the overall world (excluding the US). 27

In this regard, as far as the econometric model is concerned, we rely on the Multi-28 variate Singular Spectrum Analysis (MSSA). We are motivated to use SSA because it 29 is a non-parametric technique that works with arbitrary statistical processes, whether 30 linear or non-linear, stationary or non-stationary, Gaussian or non-Gaussian [27], and 31 being a versatile approach for modelling and forecasting time series, it has been found 32 to outperform wide-array of other forecasting models [11, 15, 17, 18]. At this stage, we 33 must also highlight that, since the ENSO data is available monthly, while the Gross 34 Domestic Product (GDP) growth data are quarterly, we rely on a mixed-frequency 35 MSSA model to forecast the growth rate, as recently developed by [20], rather than 36 averaging the ENSO data over three-months forming the quarter to prevent possi-37 ble loss of information **8**. This serves as an additional empirical novelty of our paper. 38 While forecasting is the primary focus, to highlight the underlying nonlinear and time-39 varying relationship between growth and inflation with the ENSO to motivate the SSA 40 across short-, medium- and long-runs, we also conduct an in-sample-based causality 41 analysis using the wavelet coherence approach. 42

The remainder of the paper is organized as follows: Section 2 outlines the methodologies, while Section 3 presents the data and Section 4 discusses the results. Finally, Section 5 concludes.

46 2. Methods

The investigation of the impact of the ENSO on GDP growth and inflation is carried out in two stages. First a wavelet coherence analysis is used to investigate the complex relationship between the economic series and the ENSO. Next, we use a data driven forecasting method (mixed-frequency and standard multivariate SSA), and a nonparametric test (KSPA) to test for the role of monthly ENSO for quarterly GDP growth and monthly inflation. Following is a brief review of the employed methods.

53 2.1. Continuous Wavelet Transform and Coherence Analysis

A Continuous Wavelet Transform, CWT, uses a mother wavelet $\psi(.)$ to transform a discrete-time time series $\{y_t\}_1^n$, to wavelet daughters $W(\tau, s)$, for time localizing parameter τ and scale parameter s. The wavelet daughters $W(\tau, s)$ are defined as convolution of time series $\{y_t\}_1^n$ with the localized (in time and frequency space by τ and s) mother wavelet $\psi(.)$ 4:

$$W(\tau, s) = \sum_{t} y_t \frac{1}{\sqrt{s}} \bar{\psi}(\frac{t-\tau}{s}),$$

where $\bar{\psi}(.)$ is the complex conjugate of $\psi(.)$. Larger values of scale parameter *s*, reveal the long term periodic behavior (with low frequency) and smaller values of scale parameter reveal the details in short term periodic patterns (with higher frequencies). One common choice for mother wavelet is the Morlet wavelet [24]:

$$\psi(t) = \pi^{-1/4} e^{i\omega t} e^{-t^2/2},$$

⁶³ where ω is dimension less frequency, also known as angular frequency. According to ⁶⁴ the literature, the $\omega = 6$ is the proper choice, since it makes the Morlet wavelet ⁶⁵ approximately analytic [4].

Large absolute values of $W(\tau, s)$ show the powerful periodic pattern in time τ and period s. The wavelet power spectrum of time series $\{y_t\}_1^n$ is defined as

$$Power(\tau, s) = \frac{1}{s} |W(\tau, s)|^2.$$

The power spectrum can be used to map the periodic patterns in the time series $\{y_t\}_1^n$, through time. The wavelet power spectrum can be tested against white noise spectrum, using asymptotic chi square statistic [10, 29] or Monte Carlo simulation [10, 29]. The Monte Carlo simulation approach is used in this paper.

In the bivariate case, the cross wavelet transform can be used to investigate the relation between two time series, x_t and y_t [4]:

$$W_{xy}(\tau,s) = \frac{1}{s} W_x(\tau,s) \overline{W}_y(\tau,s),$$

where $W_x(\tau, s)$ and $W_y(\tau, s)$ are the wavelet daughters in time series x_t and y_t , respectively and \overline{W} denotes complex conjugate. The wavelet cross power spectrum can be used to map the similarities between two time series' periodic behavior:

$$Power_{xy}(\tau, s) = |W_{xy}(\tau, s)|$$

⁷⁷ Using the wavelet cross power spectrum, we can map the localized correlation between ⁷⁸ two series, through time and scale. Coherence between two time series x_t and y_t is

⁷⁹ defined as the local correlation between the series, localized at time τ and scale s [4]:

$$Coherence_{xy}(\tau, s) = \frac{|sW_{xy}(\tau, s)|^2}{sPower_x(\tau, s)Power_y(\tau, s)}$$

⁸⁰ Like power spectrum, wavelet Coherence between two series can be tested using Monte

 81 Carlo simulation 29.

2.2. Standard and Mixed Frequency Multivariate Singular Spectrum 82 Analyses 83

Following is a brief review of implementing standard and mixed frequency MSSAs. 84 Since the bivariate version of the method is used in this research, the notation is 85 adapted to the two-variable case. Consider the bivariate time series $\{X_t := (x_t, y_t)\}_{t \in \mathbb{S}}$ 86 which takes values in $\mathcal{R}_{\mathbf{X}} \subseteq \mathbb{R}^2$. The index set S can be subset of either Z or N. It is 87 assumed that both series are already scaled appropriately and expressed in commensu-88 rable units of measurement. Using a observed time series of length n (i.e. $X_1, ..., X_n$) 89 and embedding dimension L, MSSA follows these steps **19**: 90

- 91
- 92

(1) We apply the hankelization operator $\mathcal{H}_{L}(.)$ to each of the component series of \boldsymbol{X}_t , and obtain the trajectory $(m \times L)$ matrices \boldsymbol{T}_i as:

$$\boldsymbol{T}_i := \mathcal{H}_L(X_{1i}, \dots, X_{ni}), \quad i = 1, 2$$

where $X_{t1} = x_t, X_{t2} = y_t$ and m = n - L + 1. Concatenate the trajectory matrices 93 horizontally, and build the $(m \times 2L)$ MSSA trajectory matrix $T_X := [T_1, T_2]$ 94 which will be used for decomposition and reconstruction in next steps. 95

- (2) We build the sample covariance matrix $C := m^{-1}T'_{X}T_{X}$, which is block sym-96 metric matrix, containing covariance and cross-covariance matrix for both com-97 ponent series of X_t . 98
- (3) Obtain eigenvalues $\lambda_1 \geq \cdots \geq \lambda_{2L}$ and eigenvectors v_1, \ldots, v_{2L} of sample covari-99 ance matrix C. Using eigenvalues and eigenvectors, one can decompose sample 100 covariance matrix as: 101

$$oldsymbol{C} = \sum_{j=1}^{2L} \lambda_j oldsymbol{v}_j oldsymbol{v}_j = oldsymbol{V} oldsymbol{\Lambda} oldsymbol{V}',$$

- where V is a $(2L \times 2L)$ matrix containing all eigenvectors of C. 102
- (4) Partitioning V appropriately in to $V = [V'_1, V'_2]'$, estimate the individual tra-103 jectory matrices as: 104

$$\hat{\boldsymbol{T}}_i(k) := \boldsymbol{T}_i \boldsymbol{Q}(k), \quad i = 1, 2,$$

where $Q(k) := \sum_{i \in \mathcal{I}_k} v_{ij} v'_{ij}$ for a subset of eigenvectors in V, i.e. $\mathcal{I}_k \subseteq \{1, ..., L\}$. 105 (5) Obtain the reconstructed series by applying diagonal average n operator $\mathcal{D}_{(L,n)}(.)$ 106 to the estimated trajectory matrices: 107

$$\left\{\hat{X}_{t,i}(k)\right\}_{t=1}^{n} := \mathcal{D}_{(L,n)}\left(\hat{\boldsymbol{T}}_{i}(k)\right)$$

Now, suppose the x_t is the time series observed in lower frequency (say quarterly) 108 and y_t is the time series observed in higher frequency (say monthly). The mixed-109 frequency MSSA introduced by **20** follows these steps: 110

(1) We build the initial observation matrix in higher frequency by repeating the val-111 ues in lower frequency. For instance, if x_t is observed quarterly (each observation 112 is belongs to the end of the quarter) and y_t is monthly, the initial observation 113

$$H^{(0)} = \begin{pmatrix} x_1 & y_1 \\ x_1 & y_2 \\ x_1 & y_3 \\ \hline x_2 & y_4 \\ x_2 & y_5 \\ \hline x_2 & y_6 \\ \hline \vdots & \vdots \end{pmatrix}_{n \times 2}, I = \begin{pmatrix} 0 \\ 0 \\ 1 \\ \hline 0 \\ 0 \\ 1 \\ \hline \vdots \end{pmatrix}_{n \times 1}$$

where n is the number of observations in time series with higher frequency. As it 115 can be seen, in each quarter, the monthly values in quarterly observed series, are 116 filled-in with the end-of-the-quarter observation. The Matrix I shows which rows 117 in matrix $H^{(0)}$ are actual quarterly observations (denoted as ones) and which 118 ones are filled with end-of-the-quarter observation (denoted as zeros). 119

(2) Using a standard MSSA 19 on matrix $H^{(0)}$ to obtain the predicted values in 120 higher frequency, namely $\hat{H}^{(0)}$. Initialize the root-mean-squared measure as the 121 root mean square of first column in $\hat{H}^{(0)}$ (the column associated with the time 122 series with lower sampling frequency): 123

$$RMSE^{(0)} = \sqrt{\frac{1}{n} \sum_{t=1}^{n} \left(\hat{h}_{t,1}^{(0)}\right)^2},$$

124

where $\hat{h}_{t,1}^{(0)}$ is the *t*th element in first column of $\hat{H}^{(0)}$. (3) In *i*th iteration, we substitute actual observations (that is the second column of 125 $H^{(0)}$ and the elements in first column which are the associated with ones in I 126 matrix) into $\hat{H}^{(i-1)}$ and build the new H matrix: 127

$$H^{(i)} = \begin{pmatrix} \hat{h}_{t,1}^{(i-1)} & y_1 \\ \hat{h}_{t,2}^{(i-1)} & y_2 \\ \underline{x_1 & y_3} \\ \underline{\hat{h}_{t,4}^{(i-1)} & y_4} \\ \hat{h}_{t,5}^{(i-1)} & y_5 \\ \underline{x_2 & y_6} \\ \hline \vdots & \vdots \end{pmatrix}_{n \times 2}$$

- (4) Applying standard MSSA to $H^{(i)}$ to obtain the new predicted values in higher 128 frequency, namely $\hat{H}^{(i)}$. 129
- (5) Obtaining a new root-mean-squared measure: 130

$$RMSE^{(i)} = \sqrt{\frac{1}{n} \sum_{t=1}^{n} \left(\hat{h}_{t,1}^{(i-1)} - \hat{h}_{t,1}^{(i)}\right)^2}.$$

(6) For some predefined small value ε , while $RMSE^{(i)} \leq RMSE^{(i-1)}$ and $|RMSE^{(i)} - RMSE^{(i-1)}| > \varepsilon$, we repeat steps (3) to (5). 131 132

114

(7) If $RMSE^{(i)} > RMSE^{(i-1)}$, consider the $\hat{H}^{(i-1)}$ as the final estimation for high frequency observation matrix and if $|RMSE^{(i)} - RMSE^{(i-1)}| \le \varepsilon$, put $\hat{H}^{(i)}$ as final estimation for high frequency observation matrix.

(8) Applying standard MSSA on \hat{H} , the final estimation for high frequency observation matrix obtained in step (7), for out-of-sample forecasting.

138 2.3. Forecasting Evaluation

¹³⁹ Suppose $E(y_{t+h}|\mathcal{F}_t)$ is the *h* step ahead forecast from MSSA and the η_{t+h} is the ¹⁴⁰ forecasting square error of the conditional mean model at time *t*:

$$\eta_{i+h} = (y_{t+h} - E(y_{t+h}|\mathcal{F}_t))^2$$
.

Kolmogorov-Smirnov Predictive Accuracy, KSPA, test **16** is used for comparing the forecasting accuracy of different models. Let $F_{\eta_{i+h}^{(k)}}(.)$ be the distribution function of square error corresponding to kth forecasting model. One tailed KSPA, tests the following hypothesis:

$$\begin{cases} H_0: F_{\eta_{i+h}^{(1)}}(z) \le F_{\eta_{i+h}^{(2)}}(z) \\ H_1: F_{\eta_{i+h}^{(1)}}(z) > F_{\eta_{i+h}^{(2)}}(z) \end{cases}$$

Rejection of the null hypothesis implies that the forecasting error of second model, $\eta^{(2)}$ is stochastically smaller than the forecasting error of the first model, $\eta^{(1)}$, i.e., the second forecasting model is significantly more accurate than the first one.

¹⁴⁸ 3. Data Description

As far as the metric of the ENSO cycle is concerned, traditionally the Southern Os-149 cillation Index (SOI) index is used.¹ The SOI gives an indication of the development 150 and intensity of El Niño or La Niña events in the Pacific Ocean. The SOI is calculated 151 using the pressure difference between Tahiti and Darwin. Sustained negative (positive) 152 values of the SOI below (above) 7(+7) often indicate El Niño (La Niña) episodes. 153 Low atmospheric pressure tends to occur over warm water and high pressure occurs 154 over cold water, in part because of deep convection over warm water. El Niño episodes 155 are defined as sustained warming of the central and eastern tropical Pacific Ocean, and 156 La Niña episodes are defined as sustained cooling of the central and eastern tropical 157 Pacific Ocean, resulting in a decrease and an increase in the strength of the Pacific 158 trade winds, respectively. 159

The reliability of the SOI, however, is considered limited due to both Darwin and Tahiti being well south of the equator, resulting in the surface air pressure at both locations being less directly related to ENSO. To overcome this issue, a new index called the Equatorial Southern Oscillation Index (EQSOI) has been created.² To generate the data for this index, two new regions centered on the equator are delimited, with

¹See: http://www.bom.gov.au/climate/enso/soi/.

 $^{^{2}\}mathrm{See}$ Anthony Barnston the discussion of of the National Oceanic and Athttps://www.climate.gov/news-features/blogs/enso/ mospheric Administration here: why-are-there-so-many-enso-indexes-instead-just-one for further details.

the western one located over Indonesia and the eastern one located over the equatorial Pacific, close to the South American coast. The EQSOI is obtained from the Climate Prediction Center (National Weather Service) of the National Oceanic and Atmospheric Administration (US Department of Commerce).³ In our analysis, we use the EQSOI index to capture the ENSO.

As far as our macroeconomic variables are concerned, data on year-on-year growth of 170 quarterly real GDP and monthly inflation rates of the US, other advanced barring the 171 US and emerging market economies, as well as the overall World economy excluding 172 the US are obtained from the Global Economic Database maintained by the Federal 173 Reserve Bank of Dallas.⁴ Data on 18 advanced (excluding the US, Japan, Germany, the 174 United Kingdom (UK), France, Italy, Spain, Canada, South Korea, Australia, Taiwan, 175 The Netherlands, Belgium, Sweden, Austria, Switzerland, Greece, Portugal, and Czech 176 Republic, in order of Purchasing Power Parity (PPP)-adjusted GDP shares in 2005) 177 and 21 emerging (China, India, Russia, Brazil, Mexico, Turkey, Indonesia, Poland, 178 Thailand, Argentina, South Africa, Colombia, Malaysia, Venezuela, Philippines, Nige-179 ria, Chile, Peru, Hungary, Bulgaria, and Costa Rica, in order of PPP-adjusted GDP 180 shares in 2005) countries are used to compile the aggregates for the blocs, by using 181 trade weights with the US in weighting the country-level data. The reader is referred 182 to **13** for further details. 183

Based on latest data availability at the time of writing this paper, the monthly analysis involving the inflation rates and the EQSOI cover the period of February 1981 to July 2021, while the real GDP growth and EQSOI span the period of June 1981 (1981:Q2) to June 2021 (2021:Q2) for the US, the advanced and world economies excluding the US, but the same for emerging markets starts a bit later from March 1984 (1984:Q1), but also ends in June 2012 (2021:Q2).

190 4. Empirical Results

Before testing the role of EQSOI in forecasting inflation and GDP growth, we use 191 CWT to investigate the underlying time-varying relation between EQSOI and the 192 macroeconomic variables for each of the four economic areas. As a measure of de-193 pendency, EQSOI's wavelet coherence with inflation and GDP growth is estimated 194 using CWT. For the GDP growth case, since we are interested in coherence between 195 the monthly EQSOI and the quarterly GDP growth, the sampling frequency for the 196 monthly series is set to 3 (i.e., 3 samples during each quarter), so the time unit in 197 the wavelet figures will correspond to a quarter. Latter, in mixed-frequency MSSA 198 (MFMSSA), we will use the original monthly data to forecast the quarterly GDP. 199

We use MSSA to forecast inflation and MFMSSA to forecast GDP growth when EQSOI is included as a predictor. For each economic area, two sets of forecasts are produced: one without using any predictor, and one using EQSOI as a predictor. Specifically, following is the list of forecasting models:

- Model 1: Forecasting inflation without any predictors; i.e., univariate forecasts using SSA.
- Model 2: Forecasting inflation using EQSOI as a predictor; i.e., bivariate forecasts using MSSA.
- 207 208

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• Model 3: Forecasting GDP growth without any predictors; i.e., univariate fore-

³https://www.cpc.ncep.noaa.gov/data/indices/. ⁴https://www.dallasfed.org/institute/dgei/gdp.aspx

209 casts using SSA.

• Model 4: Forecasting GDP growth using SOI as predictors; i.e., bivariate forecasts using MFMSSA.

Since SSA can be used with even non-stationarity data [11], [21], [22], unit root tests are not necessary to be conducted to ensure stationarity before resorting to forecasting using SSA. The KSPA test is employed to compare the accuracy of the forecasts with and without the predictor. In this regard, the null and alternative hypotheses, for comparing univariate and bivariate models associated with the KSPA test are as follows:

(1) For comparing Model 1 and Model 2 (testing for EQSOI's role in inflation fore casting):

$$\begin{cases} H_0: F_{\eta_{i+h}^{(1)}}(z) \le F_{\eta_{i+h}^{(2)}}(z) \\ H_1: F_{\eta_{i+h}^{(1)}}(z) > F_{\eta_{i+h}^{(2)}}(z) \end{cases};$$

$$(1)$$

(2) For comparing Model 3 and Model 4 (testing for EQSOI's role in GDP growth
 forecasting):

$$\begin{cases} H_0: F_{\eta_{i+h}^{(3)}}(z) \le F_{\eta_{i+h}^{(4)}}(z) \\ H_1: F_{\eta_{i+h}^{(3)}}(z) > F_{\eta_{i+h}^{(4)}}(z) \end{cases};$$
(2)

where $\eta_{i+h}^{(i)}$ is the *h*-step ahead forecasting square error corresponding to "Model i". 222 In each case, half of the data is used for estimating the SSA/(MF)MSSA, and 223 the rest is used for out-of-sample forecasting, with the KSPA test applied to the 224 out-of-sample forecasting results (with significance level set at: $\alpha = 0.05$). Rejecting 225 the null hypothesis in 1 implies that Model 2 (inflation forecasting model containing 226 EQSOI as predictor) dominates Model 1 (univariate inflation forecasting) significantly. 227 In the same manner, rejecting the null hypothesis in 2 implies that Model 3 (GDP 228 growth forecasting model containing EQSOI as predictor) dominates the null model 220 (univariate GDP growth forecasting) significantly. 230

231 4.1. Inflation Forecasting Results

Figures 1 and 2 show the monthly EQSOI and inflation time series for the four economic blocs. As can be seen, there are resemblance among the inflation time series, especially around 2008 during the Global Financial Crisis (GFC).

In order to better understand the similarities in the periodic behavior of EQSOI and inflation, a CWT is used to estimate their power spectrums over time. The estimated power spectrums are shown in figures 3 and 4 Black contours present significant power spectrums. EQSOI's power spectrum shows significant periodic behavior with the periodic length falling between 16 and 64 months, as well as periods with length around 128 months. The significant periods of EQSOI are almost steady (i.e., almost the same) over time.

Figure 4 shows the wavelet power spectrum for inflation in advanced economies (with US excluded) (top left), emerging economies (top right), the US economy (bottom left) and the world economy (with US excluded) (bottom right). As Figure 4 shows, the inflation in advanced, the US and the world economies have significant periodic

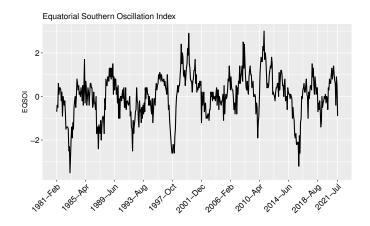


Figure 1. Monthly Equatorial Southern Oscillation Index time series.

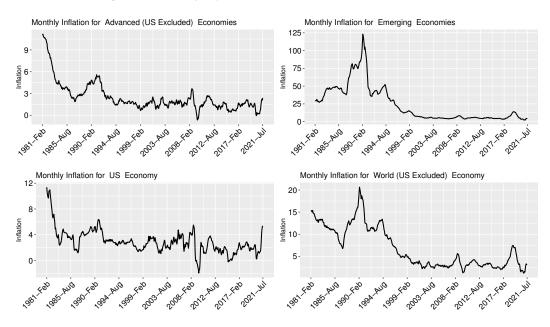


Figure 2. Top Left: Monthly Inflation time series in "Advanced Economies" (US excluded); Top Right: Monthly Inflation time series in "Emerging Economies"; Bottom Left: Monthly Inflation time series in "US Economy"; Bottom Right: Monthly Inflation time series in "World Economy" (US excluded).

behavior mostly between 32 and 128 month periods, which overlaps with those of the
EQSOI's significant periods. For emerging economies however, there is no evidence of
significant period in recent years (i.e., after 2011).

According to wavelet power spectrums, EQSOI and inflation have resemblance in their periodic behavior, in three economic areas i.e., advanced (without the US), the US and the world (with the US excluded) economies. Given this, we can suggest that, if significant correlation between the EQSOI and inflation is observed in same periods (i.e., the location where the power spectrum is significant for both EQSOI and inflation), we may be able to use one time series as a predictor to forecast the other one.

As a measure of correlation between the inflation and EQSOI, the wavelet coherences are presented in Figure 5. According to these results, there is significant wavelet

EQSOI's Monthly Wavelet Power Spectrum

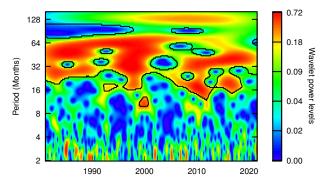


Figure 3. Equatorial Southern Oscillation (EQSOI) Index continuous monthly wavelet power spectrum. The thick black contour designates the 10% significance level.

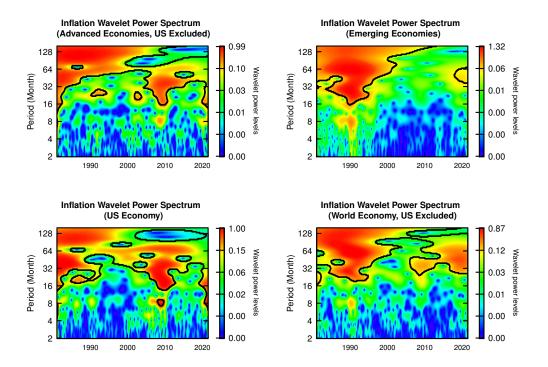


Figure 4. Top Left: Inflation's wavelet power spectrum in "Advanced Economies" (US excluded). Top Right: Inflation's wavelet power spectrum in "Emerging Economies". Bottom Left: US Inflation's wavelet power spectrum. Bottom Right: World Inflation's wavelet power spectrum (US excluded). The thick black contour designates the 10% significance level.

coherence between EQSOI and inflation (green, yellow and red areas show coherence 258 above 0.94), though not significant in most of the periods over time. The significant 259 wavelet coherence between EQSOI and Inflation occurs mostly around 32- and 64-260 month periods, in all four economic areas. However, as it is evident form Figure 5. 261 the significant coherence between EQSOI and inflation does not always correspond to 262 the location (i.e., for time and periods) with highest power spectrum. For instance, 263 in emerging economies, inflation's power spectrum around the 32-month period is not 264 significant after 2000. This means that the period in which EQSOI and inflation have 265

significant coherence, is a period which has low power (and hence low impact) on inflation's periodic pattern. In the case, where significant coherence between inflation and
EQSOI fall in the periods with high values of wavelet power spectrum in both series,
we may use EQSOI as a potential predictor for inflation forecasting (provided oscillations in EQSOI occur before inflation). But as is well-known, existence of in-sample
causality cannot guarantee that the same will hold over an out-of-sample, since the
latter is stronger test of predictability, and we consider this next.

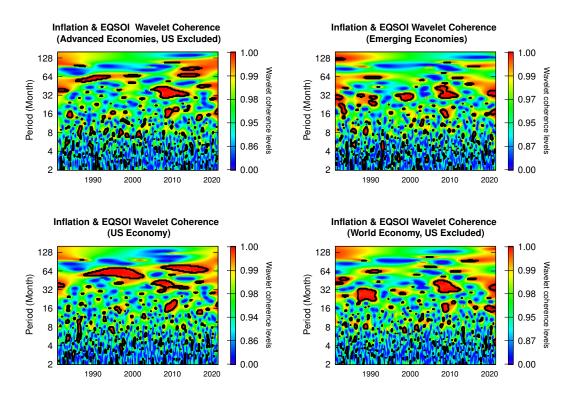


Figure 5. Top Left: Wavelet coherence between Inflation in "Advanced Economies" (US excluded) and SOI. Top Right: Wavelet coherence between Inflation in "Emerging Economies" and SOI. Bottom Left: Wavelet coherence between US Inflation and SOI. Bottom Right: Wavelet coherence between World Inflation (US excluded) and SOI. The 10% significance level is shown as a thick black contour.

272

KSPA p-values for testing the role of EQSOI in forecasting inflation (i.e., hypothesis 273 (1), for four economic areas, are presented in Table 1. According to KSPA test results, 274 using EQSOI as predictor can significantly improve inflation forecasting accuracy (i.e., 275 rejects the null hypothesis in (1) for medium- and long-term forecasting horizons, in 276 advanced and world economies (with US excluded), as well as for the US economy (i.e., 277 $h \ge 10$ in advanced economies, $h \ge 9$ in the US economy and $h \ge 7$ in world economy). 278 In emerging economies, however, using EQSOI as predictor does not improve inflation 279 forecasting accuracy (i.e., the null hypothesis in (1) is not rejected). 280

281 4.2. GDP Growth Forecasting Results

Figure 6 shows the quarterly GDP growth for the four economic areas. As it can be seen, there are similarities between the EQSOI (as presented in Figure 1) and the GDP growth rates, again especially during the GFC, just as in case of the inflation

Forecasting	Advanced	Emerging	US	World
Horizon	Economies (US excl.)	Economies	Economy	Economy (US excl.)
h = 1	1.0000	1.0000	0.9299	0.8926
h = 2	0.9820	0.9955	0.8926	0.5197
h = 3	0.9955	1.0000	0.5769	0.7476
h = 4	1.0000	1.0000	0.4103	0.6920
h = 5	0.8926	0.9955	0.2293	0.2293
h = 6	0.6920	1.0000	0.0729	0.0584
h=7	0.6347	1.0000	0.1623	0.0127^{*}
h = 8	0.2688	1.0000	0.0584	0.0007^{*}
h = 9	0.0903	1.0000	0.0127^{*}	0.0167^{*}
h = 10	$\boldsymbol{0.0052^*}$	1.0000	0.0127^{*}	0.0167^{*}
h = 11	0.0014^{*}	0.9955	0.0002^{*}	0.0071^{*}
h = 12	0.0000^{*}	1.0000	0.0000^{*}	0.0020^{*}
h = 13	0.0001^{*}	1.0000	0.0014^{*}	0.0007^{*}
h = 14	0.0000*	1.0000	0.0001^{*}	0.0038^{*}
h = 15	0.0000^{*}	1.0000	0.0003^{*}	0.0005^{*}
h = 16	0.0000*	1.0000	0.0002^{*}	0.0001^{*}
h = 17	0.0000^{*}	1.0000	0.0000^{*}	0.0002^{*}
h = 18	0.0000*	1.0000	0.0000*	0.0001^{*}
h = 19	0.0000^{*}	1.0000	0.0000^{*}	0.0000*
h = 20	0.0000*	1.0000	0.0003^{*}	0.0000*
h = 21	0.0000^{*}	0.9955	0.0003^{*}	0.0000*
h = 22	0.0000*	0.9599	0.0000*	0.0000*
h = 23	0.0000^{*}	0.9599	0.0002^{*}	0.0001^{*}
h = 24	0.0000*	0.9599	0.0002*	0.0000*

Table 1. KSPA test p-values for testing the EQSOI effect on inflation forecasting accuracy, Hypothesis (1).

.* EQSOI improves the inflation forecasting accuracy, significant (at $\alpha = 0.05$ level).

285 rates.

Figure 7 shows the quarterly measured wavelet power spectrum for the EQSOI (with the sampling frequency set to 3 in time unit, since there are three monthly observations in each quarter). Significant power spectrums are shown with black contour lines. As the EQSOI's wavelet power spectrum shows, there are significant mid- and long-range (longer than 8 quarters) periodic pattern in the EQSOI, which is basically the same as the monthly measured power spectrum (presented in Figure 3).

Figure 8 shows the wavelet power spectrum for GDP growth in "Advanced 292 Economies (US excluded)", (top left), "Emerging Economies" (top right), "US Econ-293 omy" (bottom left) and "World Economy (US excluded)" (bottom right). As it can 294 be seen in Figurer 8, steady GDP growth significant periodic patterns mostly fall in 295 the midrange (between 8 and 16 quarters) and long periods (around 32 quarters), 296 which overlaps with the EQSOI's periodic pattern, especially in mid-range periods. In 297 general, the GDP growth power spectrums in all four economic areas show significant 298 periodic behavior that has similarities with the EQSOI through time. 299

The wavelet coherences between the GDP growth rates and the EQSOI are presented in Figure 9, Figure 9, shows that there is high wavelet coherence between the

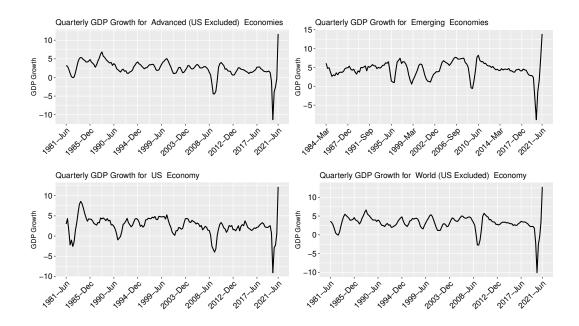


Figure 6. Quarterly GDP growth time series for "Advanced Economies (US excluded)", top left; "Emerging Economies", top right; "US Economy", bottom left; "World Economy (US excluded)", bottom right.

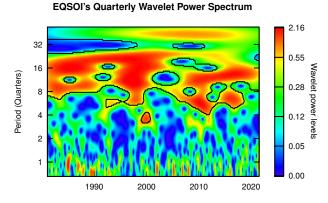


Figure 7. Equatorial Southern Oscillation (EQSOI) Index continuous quarterly wavelet power spectrum; The thick black contour designates the 10% significance level.

EQSOI and GDP growth rates (green, yellow and red areas show coherence above 302 0.94). However, the significant wavelet coherence between the EQSOI and the GDP 303 growth occur mostly in midrange periods (around 8 and 16 quarters), in all economic 304 areas. Furthermore, according to Figure 9, the coherence between EQSOI and the 305 GDP growth is observed to be stronger before 2000s in the "Advanced Economies", 306 the "US Economy" and the "World Economy", as evident from large red areas on 307 the left side of time axis in the top left, the bottom left and the bottom right panels 308 of Figure 9. According to CWT results, as is evident from figures 8 and 9, the GDP 309 growth have similarities with EQSOI in power spectrums, and there exist significant 310 wavelet coherence between them. Since the significant coherence between the two se-311 ries is located in the areas with significant power spectrum in both series, the EQSOI 312 can be considered as a potential predictor in forecasting GDP growth rates, but for 313

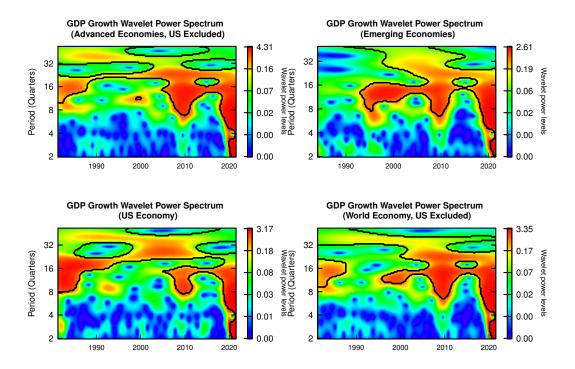


Figure 8. GDP growth wavelet power spectrum for "Advanced Economies (US excluded)", top left; "Emerging Economies", top right; "SU Economy", bottom left; "World Economy (US excluded)", bottom right; The thick black contour designates the 10% significance level.

this to happen, the oscillation in the EQSOI need to occur well enough before it is observed in the GDP growth rates. But again in-sample predictability is no guarantee for out-of-sample forecasting gains, and it is the latter which we turn to next.

Table 2 show the results of quarterly GDP growth forecasting using SSA and 317 MFMSSA with and without EQSOI as predictor respectively. As can be seen, the 318 bivariate forecasting model (the model using EQSOI as a predictor) significantly im-319 proves the GDP growth forecasting accuracy in advanced and world economies (with 320 US excluded), mostly at the short-term, and also at certain medium- and long-run 321 horizons (i.e. h = 1, ..., 6, 16, 24 for the former, and h = 1, ..., 8, 15 and 16 for 322 the latter). For emerging economies, EQSOI significantly improves GDP growth fore-323 casting accuracy at very short (h = 1) and medium-term (h = 14, ..., 17) horizons. 324 Interestingly for the US GDP growth forecasting, EQSOI as predictor does not provide 325 significant forecasting gains at any horizon. 326

327 5. Conclusion

In this paper, for the first time, the role of the ENSO, as captured by the EQSOI index is used to formally forecast the inflation and GDP growth rates of not only the US economy, but advanced (excluding the US) and emerging countries, as well as for the world economy (barring the US). For our purpose, we use univariate and multivariate SSA, as well as mixed-frequency version of the latter since the EQSOI is monthly, while GDP growth is available only at quarterly frequency unlike monthly inflation rates.

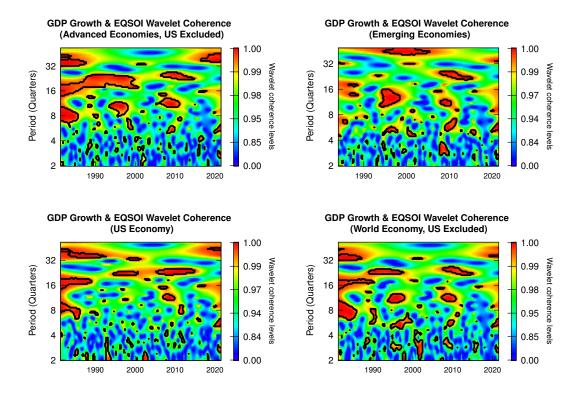


Figure 9. Wavelet coherence between GDP growth and SOI. "Advanced Economies (US excluded)", top left; "Emerging Economies", top right; "SU Economy", bottom left; "World Economy (US excluded)", bottom right; The 10% significance level is shown as a thick black contour.

As a preliminary analysis to motivate the use of the SSA method which is a model-335 free approach, we also use the wavelet coherence to depict complex time-varying rela-336 tionships between the macro variables and the EQSOI. Since in-sample predictability 337 does not guarantee the same for the out-of-sample, we then turned to the SSA method 338 to show that the EQSOI significantly improves the forecasting accuracy of the inflation 339 rates at medium- and long-runs for the advanced and world economies (when the US is 340 excluded), as well as for the US economy. For inflation rate of the emerging economies 341 however, the use of the EQSOI as predictor does not produce forecasting gains. At the 342 same time, GDP growth forecasting results show that using the EQSOI as predictor 343 significantly improves accuracy in advanced (with US excluded) and emerging coun-344 tries, as well as for the world economy (excluding the US). For these country groups, 345 the improvement is mostly evident in short horizons, as well as certain medium and 346 long-runs for advanced and world economies (when US is excluded), and very short as 347 well as for the medium-term associated with emerging economies. Interestingly, using 348 EQSOI as predictor does not improve the forecasting accuracy of US GDP growth. In 349 sum, the ENSO tend to predict both in- and out-of-sample inflation and GDP growth 350 rates globally, though there are exceptions in terms of forecasting of the inflation rate 351 of emerging economies and the growth rate of the US. These contrasting results for 352 the emerging markets and the US in terms of forecastability of output growth and 353 inflation respectively emanating from the EQSOI, seems to be indicative of the strong 354 reliance of emerging countries on agriculture (and its corresponding high share in 355 GDP), and the US being the highest importer in the overall of commodity market. 356

Forecasting	Advanced	Emerging	US	World
Horizon	Economies (US excl.)	Economies	Economy	Economy (US excl.)
h = 1	0.0034 *	0.0000*	0.6449	0.0000*
h = 2	0.0018 *	0.0594	0.4233	0.0063^{*}
h = 3	0.0063 *	0.6125	0.6449	0.0009^{*}
h = 4	0.0002 *	0.3826	0.1730	0.0034^{*}
h = 5	0.0034 *	0.4937	0.4233	0.0002^{*}
h = 6	0.0321 *	0.4937	0.4233	0.0009^{*}
h = 7	0.2415	0.4937	0.6449	0.0063^{*}
h = 8	0.5318	0.6125	0.4233	0.0321^{*}
h = 9	0.6449	0.4937	0.3254	0.0516
h = 10	0.6449	0.2851	0.7553	0.0516
h = 11	0.7553	0.2043	0.6449	0.0516
h = 12	0.3254	0.1407	0.6449	0.0516
h = 13	0.2415	0.0932	0.9322	0.0516
h = 14	0.3254	0.0364^{*}	0.8539	0.0516
h = 15	0.3254	0.0364^{*}	0.8539	0.0018^{*}
h = 16	0.0193^{*}	0.0364^{*}	0.4233	0.0112^{*}
h = 17	0.0800	0.0214^{*}	0.4233	0.0516
h = 18	0.1197	0.1407	0.4233	0.1197
h = 19	0.5318	0.3826	0.6449	0.1197
h = 20	0.6449	0.2043	0.8539	0.2415
h = 21	0.3254	0.3826	0.9322	0.4233
h = 22	0.3254	0.3826	0.9322	0.7553
h = 23	0.1730	0.2851	0.9322	0.5318
h = 24	0.0321^{*}	0.2043	0.8539	0.6449

Table 2. KSPA test p-values for testing the SOI effect on GDP growth forecasting accuracy, Hypothesis (2).

.* EQSOI improves GDP growth forecasting accuracy, significant (at $\alpha = 0.05$ level).

³⁵⁷ Clearly, these findings associated with forecasts of inflation and growth due to the El
³⁵⁸ Niño and La Ninña events will allow policymakers to design monetary policy decisions
³⁵⁹ to circumvent business cycle downturns and inflationary episodes.

As part of future research, it would be interesting to extend our analysis to study individual countries rather than advanced and emerging economies as blocs, since there is lot of heterogeneity within these countries. Furthermore, one can also analyze the role of the ENSO cycle for forecasting asset prices, given that climate risks are known to affect financial markets [12].

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